Fourth Semester B.E. Degree Examination, Dec.2014/Jan.2015 **Field Theory**

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, selecting atleast TWO questions from each part.

PART - A

State and explain the Coulomb's law of electrostatic force between two point charges. 1

- A point charge $Q_1 = 25$ nC is located at $P_1(4, -27)$ and a charge $Q_2 = 60$ nC is at $P_2(-3, 4, -2)$ in free space. Find electric field \vec{E} at $P_3(1, 2, 3)$.
- Evaluate both sides of the divergence theorem for the field $\vec{D} = 2xy\vec{a}_x + x^2\vec{a}_y c/m^2$, the surface is a rectangular parallelepiped formed by planes x = 0 and x = 1, y = 0 and y = 2 and (10 Marks) z = 0 and z = 3.
- Find the potential V due to a line charge density ρ_1 c/m, bent in the form of a circular ring of 2 radius 'a'.
 - Given the potential $V = 2x^2y 5z$. Determine the expression for electric field intensity \bar{E} , the flux density \vec{D} and volume charge density ρ_v . Find the numerical values of V, E, D, ρ_v at a given point P(-4, 3, 6). Given $\epsilon_0 = 8.854 \times 10^{-12}$ F/m.
 - Define capacitance and evaluate capacitance of two concentric spherical conducting shells (05 Marks) of radius a and b with b > a.
- Derive Poisson's and Laplace's equation. 3

(06 Marks)

State and prove uniqueness theorem. b.

(08 Marks)

- Find the capacitance of a co-axial cable with inner radius a and outer radius b where b > a, (06 Marks) using Laplace equation.
- State and explain Biot-Savart law. a.

(05 Marks)

- Calculate vector current density at a given point P(2, 3, 4) if $\vec{H} = x^2 z \vec{a}_v y^2 x \vec{a}_z$. (05 Marks)
- State Ampere's circuital law. Apply it to a co-axial cable with inner conductor of radius 'a' carrying current I. The outer conductor carries return current -I. The inner radius of outer conductor is 'b' and its outer radius is 'c'. Evaluate magnetic field intensity. (10 Marks)

PART - B

- Derive the equation for force between two differential current carrying elements. (06 Marks)
 - Explain the terms magnetization and permeability.

(06 Marks)

- Derive the boundary condition between two isotropic homogeneous materials with (08 Marks) permeability μ_1 and μ_2 .
- State and explain Faraday's law.

(06 Marks) (08 Marks)

- Write Maxwell's equation in integral and point form for time varying fields. b.
- (06 Marks)

Derive the concept of displacement current density.

- 7 a. Derive the wave equation for uniform plane wave propagation in perfect dielectric and explain the concept of loss tangent. (10 Marks)
 - b. Derive the wave equation for uniform plane wave propagation in perfect conductor and explain the concept of skin effect. (10 Marks)
- 8 a. Derive reflection coefficient and transmission coefficient equations for a uniform plane wave incident normally at the boundary. (10 Marks)
 - b. Two media are characterized by intrinsic impedances $\eta_1 = 100\Omega$ and $\eta_2 = 300\Omega$ respectively. For a incident electric field of magnitude 100 v/m calculate reflected and transmitted wave magnitude. Calculate the value of standing wave ratio. (10 Marks)