

## Fourth Semester B.E. Degree Examination, June/July 2013

### Field Theory

Time: 3 hrs.

Max. Marks:100

**Note: Answer FIVE full questions, selecting at least TWO questions from each part.**

#### PART – A

1. a. State and explain Coulomb's law of force between the two point charges. Also indicate the units of quantities in the force equation. (05 Marks)  
 b. State and apply Gauss law to obtain an expression for the electric field intensity due to an infinite sheet of charge with a surface charge density  $\rho_s$  C/m<sup>2</sup> and area A m<sup>2</sup>. (10 Marks)  
 c. Find : i) Electric field intensity and ii) Electric flux density at the origin due to  $Q_1 = 0.35 \mu\text{C}$  at (0, 4, 0) m and  $Q_2 = -0.55 \mu\text{C}$  at (3, 0, 0) m. (05 Marks)
2. a. Explain with mathematical expressions: i) Potential difference ii) Absolute potential iii) Potential gradient. (06 Marks)  
 b. Derive an expression for the equation of continuity of current. (06 Marks)  
 c. At the boundary between glass ( $\epsilon_r = 4$ ) and air, the lines of electric field make an angle of 40° with normal to the boundary. If electric flux density in air is  $0.25 \mu\text{C}/\text{m}^2$ , determine the orientation and magnitude of, i) Electric flux density and ii) Electric field intensity, in glass. (08 Marks)
3. a. Derive Poisson's and Laplace equations starting from point form of Gauss law. (06 Marks)  
 b. Using Laplace equation derive an expression for the capacitance of a concentric spherical capacitor. The inner spherical conductor is of radius 'a' and potential V, while outer conductor is of radius 'b' and potential zero. (08 Marks)  
 c. Determine whether or not the following potential fields satisfy Laplace's equation :  
 i)  $V = 2x^2 - 3y^2 + z^2$  ii)  $V = r^2 + z^2$  (06 Marks)
4. a. Write an explanatory note on Biot Savart's law. (04 Marks)  
 b. Discuss the concept of scalar and vector magnetic potential and arrive at the expressions for Poissons equation in magnetostatics. (08 Marks)  
 c. State and prove ampere's circuital law and apply it to a straight solid conductor to calculate the magnetic field intensity. (08 Marks)

#### PART – B

5. a. Find the expression for the force on differential current carrying elements. (06 Marks)  
 b. Define Lorentz force equation and mention the application of its solution. (06 Marks)  
 c. Calculate the inductance of a Solenoid of 200 turns wound tightly on a cylindrical tube of length 60 cm and of diameter 6 cm, with air as media. Derive the expression used. (08 Marks)

- 6 a. With necessary relationships, explain Faradays law of electromagnetic induction for both static and time varying conditions. (10 Marks)
- b. Starting from Faradays law of electromagnetic induction derive  $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$ . (06 Marks)
- c. Find the frequency at which conduction current density and displacement current density are equal in a medium with  $\sigma = 2 \times 10^{-4}$  s/m and  $\epsilon_r = 81$ . (04 Marks)
- 7 a. What is uniform plane wave? Explain its propagation in free space with necessary equation. (08 Marks)
- b. Define skin depth and depth of penetration. (08 Marks)
- c. For copper the conductivity is 58 mega-s/m. Find the skin depth at a frequency of 10 MHz. (04 Marks)
- 8 a. With necessary equations, explain standing wave ratio. (10 Marks)
- b. Find whether the wet, marshy soil characterized by  $\sigma = 10^{-2}$  s/m,  $\epsilon_r = 15$  and  $\mu_r = 1$  may be considered as a conductor, a dielectric or neither for the frequencies: i) 60 Hz ii) 1 MHz  
iii) 100 MHz iv) 10 GHz. (10 Marks)

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